

# Combining SAR tomography and a PSI approach for high-resolution 3-D imaging of an urban area

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## Abstract

Combining persistent scatterer interferometry (PSI) and SAR tomography approaches has the potential to overcome lay-over scenarios in urban areas and may thus increase the level of detail of differential interferometric measurements of displacements in such environments. In this paper, we report the current status and results of our efforts to integrate SAR tomography into an operational interferometric point target analysis (IPTA) processing tool as an extension to the conventional persistent scatterer interferometry approach. In particular, the PSI and the SAR tomography processing approaches applied are highlighted. In addition, details in the form of tomographic slices of two high-rise buildings are presented as well as a 3-D point cloud reconstruction of parts of the city of Barcelona are shown, as extracted from an interferometric stack of high-resolution stripmap-mode SAR data at X-band acquired by the TerraSAR-X spaceborne SAR sensor.

## 1 Introduction

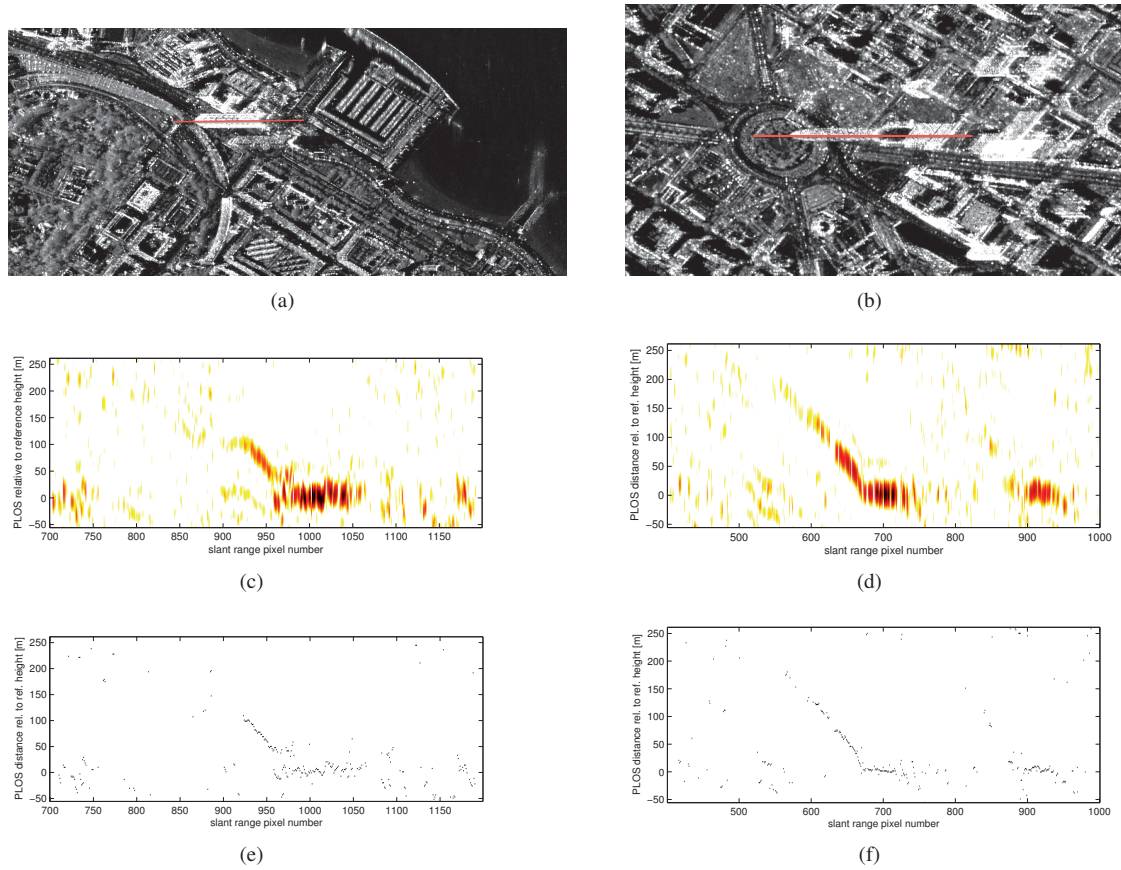
Interferometric stacks of high resolution synthetic aperture radar (SAR) data over urban areas yield a high number of scatterers that are stable over a long time span. The high resolution also leads to a higher probability of multiple temporally coherent scatterers occurring in the same range-azimuth resolution cell. Conventional persistent scatterer interferometry is based on the assumption that only one scatterer is present in a particular resolution cell. SAR tomography has the potential to overcome this restriction. In this contribution, we explore a TerraSAR-X stack over the city of Barcelona in terms of computationally efficient approaches such as Tikhonov-regularized inversion for tomographic focusing and a local peak detection for detection of scatterer localization.

Exploitation of the elevation dimension through SAR tomography approaches adds valuable information about the structure of complex target scenarios. Potential example applications include forest parameter retrieval, retrieval of structure information in urban areas, and retrieval of additional coherent targets in such scenarios. 3-D tomographic processing of such scenarios from multibaseline SAR data has been addressed and discussed by a number of authors [1–4] and [5–12]. In the spaceborne case, ideally 25–50 or up to 100 repeat-pass interferometric data sets of the same area with spatial baselines perpendicular to the line of sight are required to resolve targets also in the elevation direc-

tion, or potentially even in space and time. In this paper we show the status and results of our efforts to integrate SAR tomography into an operational interferometric point target analysis (IPTA) software as an extension to the conventional persistent scatterer interferometry approach.

## 2 Methods

The repeat-pass nature of the spaceborne interferometric stack requires that, prior to be able to perform SAR tomography in the elevation direction, a PSI processing sequence is performed to extract and remove the atmospheric phase contributions [13]. This preprocessing sequence comprises of the selection of a reference scene from stack of single-look complex (SLC) images, geocoding the data using the multilook intensity image of the reference scene, and coregistration including a refinement step using offset estimates between the data sets of the stack. After a preselection of point target candidates, based on spectral diversity and the temporal variability of the backscattering, point differential interferograms are calculated, iteratively. The topographic and orbital phases are then simulated and subtracted from the point-wise complex-valued interferogram followed by unwrapping and filtering to isolate the spatially correlated phase contributions from high-frequency phase contributions such as the residual topographic phase. If an acceptable PSI solution has been reached, the low-



**Figure 1:** Top row: Subsets of the temporally averaged intensity image of the TerraSAR-X interferometric stack showing the layover situation for a tower close to the Olympic Village in Barcelona (a) and for the Torre Agbar and surrounding buildings (b). Middle row: Tomographic slices showing the resolved extended layover situation in the slant range / elevation plane for the tower near the Olympic Village (c) and the Agbar Tower (d). Tomographic focusing algorithm: single-look Tikhonov-regularized inversion. Bottom row (e) and (f): The associated extracted locations of stable scatterer candidates using a 2-peak detector.

frequency phase contributions are expanded to the full SLCs again, such that tomographic focusing can potentially be performed at each pixel location in the SLC to find multiple scatterers in one range-azimuth resolution cell.

In the following, the system model and the tomographic inversion approaches are sketched.

The complex reflectivity  $s$  of a point target source can be described as

$$s = \alpha e^{i\phi}, \quad (1)$$

where  $\alpha$  is the amplitude and  $\phi$  is the phase of  $s$ . So the complex demodulated signal vector  $\mathbf{y}$  for that particular source  $s$  yields

$$\mathbf{y} = \mathbf{a}s \quad (2)$$

where  $\mathbf{a} = [1 e^{i\varphi_2} \dots e^{i\varphi_K}]^T$  is the steering vector with  $\varphi_m = -2k_c(r_m - r_1)$ ,  $m = 1 \dots K$ ;  $k_c$  is the central wavenumber and  $r_m$  is the range distance from the point scatterer to the  $m$ -th sensor position.

Then, for  $p$  point target sources the signal vector  $\mathbf{y}$ , which represents the signal impinging on the antenna array syn-

thesized by the different locations of the various SLC acquisition in elevation direction is

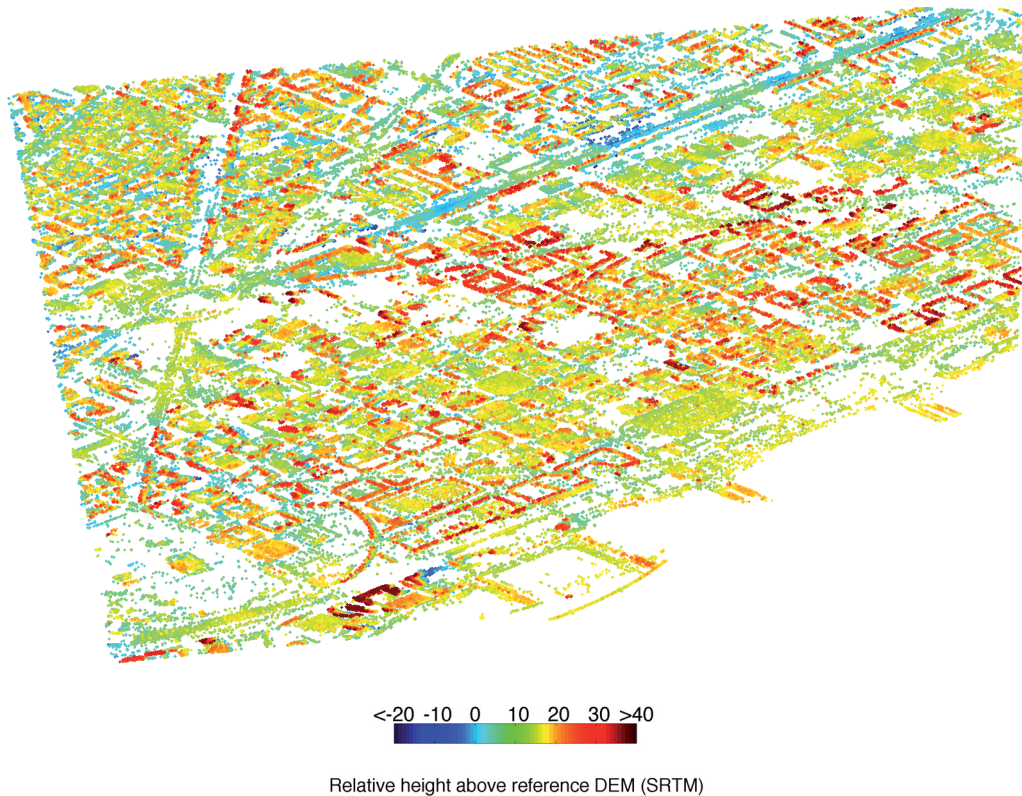
$$\mathbf{y} = [\mathbf{a}_1 \quad \dots \quad \mathbf{a}_p] \begin{bmatrix} s_1 \\ \vdots \\ s_p \end{bmatrix} = \mathbf{B}\mathbf{s}. \quad (3)$$

The matrix  $[\mathbf{a}_1 \dots \mathbf{a}_p]$  is translated to matrix  $\mathbf{B}$  called the steering matrix.

A straight-forward reconstruction—the beamforming case—of the complex reflectivity  $\hat{\mathbf{s}}$  along the elevation direction is obtained by

$$\hat{\mathbf{s}} = \mathbf{B}^H \mathbf{y} \quad (4)$$

The sampling of the tomography data is non-uniform in the elevation direction. Therefore the reconstructed tomographic profile is typically affected by spurious side lobes. A method that provides a regularized tomographic inversion is the truncated singular value decomposition (TSVD) approach as it has been suggested and applied in the context of SAR tomography in [14]. It starts with a singular



**Figure 2:** Extracted 3-D point cloud based on Tikhonov-regularized tomographic inversion of a stack of 45 stripmap-mode TerraSAR-X single look complex images acquired over the city of Barcelona. The colour coding indicates the height of the scatterer relative to the SRTM height model, which is used as a reference.

value decomposition of the steering matrix  $\mathbf{B} = \mathbf{U}\mathbf{\Sigma}\mathbf{V}^H$ . A noise threshold is set at the  $Q$ -th singular value as a function of the decay pattern of the singular values  $\sigma_n$  in the diagonal matrix  $\mathbf{\Sigma}$ . All singular values  $\sigma_n, n = Q + 1, \dots, K$  that lie below this threshold, as well as their corresponding orthogonal vectors  $\mathbf{u}_n, \mathbf{v}_n$ , are discarded. The tomographic profile is then calculated by means of the truncated pseudo-inverse  $\mathbf{V}_{1,Q}(\mathbf{\Sigma}^{-1})_{1,Q}\mathbf{U}_{1,Q}^H$  of the steering matrix  $\mathbf{B}$ :

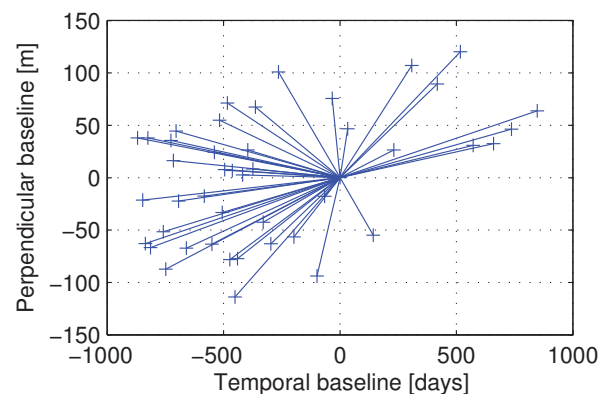
$$\hat{\mathbf{s}} = \mathbf{V}_{1,Q}(\mathbf{\Sigma}^{-1})_{1,Q}\mathbf{U}_{1,Q}^H\mathbf{y} \quad (5)$$

$\mathbf{B}$  is the steering matrix of size  $K \times N_r$ , where  $K$  is the number of acquisitions and  $N_r$  is the number of the regularly sampled positions of the tomographic profile in elevation direction.

Another approach to regularize the inversion is the Tikhonov-regularization. Instead of cutting the noise space the inverse singular values  $\sigma_{n_{rt}}^{-1}$  are weighted according to the following scheme

$$\sigma_{n_{rt}}^{-1} = \frac{\sigma_n}{\sigma_n^2 + \epsilon^2}, \quad \epsilon = \sqrt{\frac{K}{K-Q} \sum_{n=Q+1}^K |\mathbf{U}_{Q+1,K}^H \mathbf{y}|^2} \quad (6)$$

where  $\epsilon^2$  is the noise power level estimated from the projection of the measured data to the noise space [4].



**Figure 3:** Temporal vs. perpendicular spatial baseline with respect to the reference track.

### 3 Data

An interferometric stack of TerraSAR-X stripmap-mode data over the city of Barcelona is used for the combined PSI and tomographic processing. The single-reference stack consists of 45 SLCs that were acquired between 2008 and 2012. In Fig. 3, the temporal and spatial perpendicular baseline distribution of the data tomographic data set is visualized.



## 4 Results

Figs. 1 (a) and (b) show two excerpts of the TerraSAR-X data set over the city of Barcelona as a temporally averaged multi-look intensity image. In Figs. 1 (c) and (d) the corresponding tomographic transects in range/elevation depicting the tomographically resolved layover situation given by the two high-rise buildings are shown. Figs. 1 (e) and (f) show the extracted point target locations as obtained from the tomographic profiles in elevation direction. In Fig. 2 a 3-D point cloud of a larger district of Barcelona is shown as extracted using threshold-aided peak-finding within the tomographic profiles.

## 5 Discussion and Outlook

The tomographic slices in the elevation direction, obtained based on Tikhonov-regularized tomographic inversion, show that the layover situation induced by the high-rise buildings is resolved with a good side-lobe suppression. The Tikhonov-regularized inversion is computationally efficient; a drawback is the limited resolution compared to, e.g., compressive sensing approaches, which in contrast are computationally expensive. The 3-D point cloud extracted from the tomographic inversion of the stack of TerraSAR-X data shows a tomographic reconstruction of a district of Barcelona revealing a high level of detail of building structures and infrastructure features. The processing scheme presented is currently undergoing a consolidation phase, in which the benefit of the combined PSI/tomography approach in terms of an improved deformation monitoring in the context of the IPTA processing scheme [13] is further investigated.

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